



# Cambridge International AS & A Level

CANDIDATE  
NAME

--

CENTRE  
NUMBER

--	--	--	--	--

CANDIDATE  
NUMBER

--	--	--	--



## FURTHER MATHEMATICS

9231/03

Paper 3 Further Mechanics

For examination from 2020

SPECIMEN PAPER

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity ( $g$ ) is needed, use  $10 \text{ ms}^{-2}$ .

### INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **14** pages. Blank pages are indicated.





2 A light elastic string has natural length  $a$  and modulus of elasticity  $24mg$ . One end of the string is attached to a fixed point  $A$ . The other end of the string is attached to a particle of mass  $2m$ .

(a) Find, in terms of  $a$ , the extension of the string when the particle hangs freely in equilibrium below  $A$ . [2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

(b) The particle is released from rest at  $A$ .

Find, in terms of  $a$ , the distance of the particle below  $A$  when it first comes to instantaneous rest. [6]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

A series of horizontal dotted lines for writing.



.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

It is now given that  $k = 0.01$ . The speed of  $P$  when  $x$  becomes large approaches  $V \text{ m s}^{-1}$ .

- (b) (i)** Find  $V$  correct to 2 decimal places. [1]

.....

.....

.....

.....

- (ii)** Hence find how far  $P$  has fallen when its speed is  $\frac{1}{2}V \text{ m s}^{-1}$ . [2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....











- 6 A particle  $P$  is projected with speed  $u$  at an angle  $\alpha$  above the horizontal from a point  $O$  on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of  $P$  from  $O$  at a subsequent time  $t$  are denoted by  $x$  and  $y$  respectively.

(a) Derive the equation of the trajectory of  $P$  in the form

$$y = x \tan \alpha - \frac{gx^2}{2u^2} \sec^2 \alpha. \quad [3]$$

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

- (b) The greatest height of  $P$  above the plane is denoted by  $H$ . When  $P$  is at a height of  $\frac{3}{4}H$ , it has travelled a horizontal distance  $d$ .

Given that  $\tan \alpha = 2$ , find, in terms of  $H$ , the two possible values of  $d$ . [6]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

A series of 25 horizontal dotted lines spanning the width of the page, providing a template for writing.

