

CANDIDATE
NAME

--

CENTRE
NUMBER

--	--	--	--	--

CANDIDATE
NUMBER

--	--	--	--

FURTHER MATHEMATICS

9231/02

Paper 2

For Examination from 2017

SPECIMEN PAPER

3 hours

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF10)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

Where a numerical value is necessary, take the acceleration due to gravity to be 10 m s^{-2} .

The use of a calculator is expected, where appropriate.

Results obtained solely from a graphic calculator, without supporting working or reasoning, will not receive credit.

You are reminded of the need for clear presentation in your answers.

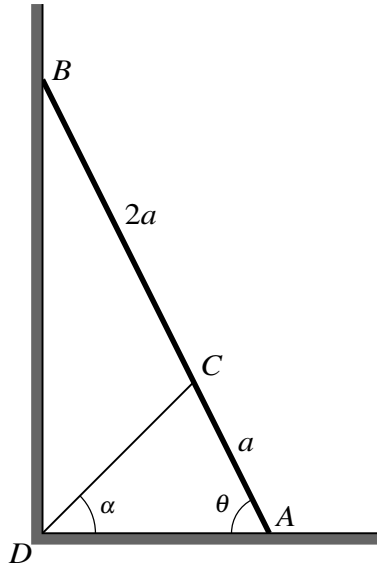
At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

This document consists of **21** printed pages and **1** blank page.



1



A uniform ladder AB , of length $3a$ and weight W , rests with the end A in contact with smooth horizontal ground and the end B against a smooth vertical wall. One end of a light inextensible rope is attached to the ladder at the point C , where $AC = a$. The other end of the rope is fixed to the point D at the base of the wall and the rope DC is in the same vertical plane as the ladder AB . The ladder rests in equilibrium in a vertical plane perpendicular to the wall, with the ladder making an angle θ with the horizontal and the rope making an angle α with the horizontal (see diagram). It is given that $\tan \theta = 2 \tan \alpha$. Find, in terms of W and α , the tension in the rope and the magnitudes of the forces acting on the ladder at A and at B . [9]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

Dotted lines for writing.

- 2 A small uniform sphere A , of mass $2m$, is moving with speed u on a smooth horizontal surface when it collides directly with a small uniform sphere B , of mass m , which is at rest. The spheres have equal radii and the coefficient of restitution between them is e .

(i) Find expressions for the speeds of A and B immediately after the collision. [4]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

Subsequently B collides with a vertical wall which is perpendicular to the direction of motion of B . The coefficient of restitution between B and the wall is 0.4 . After B has collided with the wall, the speeds of A and B are equal.

(ii) Find e . [2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

(iii) Initially B is at a distance d from the wall. Find the distance of B from the wall when it next collides with A . [4]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

3 *A* and *B* are two fixed points on a smooth horizontal surface, with $AB = 3a$ m. One end of a light elastic string, of natural length a m and modulus of elasticity mg N, is attached to the point *A*. The other end of this string is attached to a particle *P* of mass m kg. One end of a second light elastic string, of natural length ka m and modulus of elasticity $2mg$ N, is attached to *B*. The other end of this string is attached to *P*. It is given that the system is in equilibrium when *P* is at *M*, the mid-point of *AB*.

(i) Find the value of k . [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

(ii) The particle *P* is released from rest at a point between *A* and *B* where both strings are taut. Show that *P* performs simple harmonic motion and state the period of the motion. [5]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

- (iii) In the case where P is released from rest at a distance $0.2a$ m from M , the speed of P is 0.7 m s^{-1} when P is $0.05a$ m from M . Find the value of a . [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

4 A particle P of mass m is attached to one end of a light inextensible string of length a . The other end of the string is attached to a fixed point O . When P is hanging at rest vertically below O , it is projected horizontally. In the subsequent motion P completes a vertical circle. The speed of P when it is at its highest point is u .

(i) Show that the least possible value of u is \sqrt{ag} . [2]

.....
.....
.....
.....
.....

It is now given that $u = \sqrt{ag}$. When P passes through the lowest point of its path, it collides with, and coalesces with, a stationary particle of mass $\frac{1}{4}m$.

(ii) Find the speed of the combined particle immediately after the collision. [4]

.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....
.....

In the subsequent motion, when OP makes an angle θ with the upward vertical the tension in the string is T .

(iii) Find an expression for T in terms of m , g and θ . [5]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

(iv) Find the value of $\cos \theta$ when the string becomes slack. [2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

6 A biased coin is tossed repeatedly until a head is obtained. The random variable X denotes the number of tosses required for a head to be obtained. The mean of X is equal to twice the variance of X .

(i) Show that the probability that a head is obtained when the coin is tossed once is $\frac{2}{3}$. [2]

.....

.....

.....

.....

.....

(ii) Find $P(X = 4)$. [1]

.....

.....

.....

(iii) Find $P(X > 4)$. [2]

.....

.....

.....

(iv) Find the least integer N such that $P(X \leq N) > 0.999$. [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

(ii) Find the median value of Y .

[2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

(iii) Find the expected value of Y .

[2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

A series of 25 horizontal dotted lines for writing.

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.