## MARK SCHEME for the May/June 2014 series

## 4024 MATHEMATICS (SYLLABUS D)

4024/22 Paper 2, maximum raw mark 100

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2014 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

\begin{tabular}{|c|c|c|c|}
\hline \multicolumn{3}{|l|}{\begin{tabular}{c|c} 
Page 2 \& Mark Scheme \\
\& GCE O LEVEL - May/June 2014
\end{tabular}} \& \[
\frac{\text { Syllabus }}{4024}
\] \\
\hline Question \& Answers \& Mark \& art mark \\
\hline \begin{tabular}{l}
1 (a) \\
(b) \\
(c) \\
(d) (i)
\end{tabular} \& \begin{tabular}{l}
138 to 140 \\
\(D\) marked at intersection of correct arcs \\
\(103^{\circ}\) \\
\(P\) and \(Q\) marked at intersection of perpendicular bisector and circle \\
\(249^{\circ}\)
\end{tabular} \& 1
2

1
1
3

1 \& | B1 for a correctly positioned $D$ with one correct construction arc or no correct arcs Or, provided $D$ to the west of $A B$ B1 for $D$ on one correct arc or radii 5 cm and 6 cm reversed with arcs Or, provided $D$ to the east of $A B$ B1 for $D$ on intersection of two correct construction arcs |
| :--- |
| Tolerance $\pm 2^{\circ}$ |
| B1 for perpendicular bisector of $A C$ minimum 3 cm long |
| B1 for arcs radius 4.5 cm centre $B$, minimum 3 cm long cumulatively B1 for $P$ and $Q$ at correct positions |
| Tolerance $\pm 2^{\circ}$ | <br>

\hline 2 \& 97

\[
$$
\begin{aligned}
& (c= \pm) \sqrt{\frac{4 f+d}{6}} \\
& x \geq 2 \text { cao } \\
& (3+5 x)(3-5 x) \text { oe } \\
& (8 p-3 q)(x-2 y) \text { oe seen isw }
\end{aligned}
$$

\] \& | 2 |
| :--- |
| 2 |
| 1 |
| 2 | \& | M1 for $4 f=6 c^{2}-d$ or better |
| :--- |
| B1 for final answer $\{+$ or -$\} x^{*}\{+$ or -$\} 2$, where * can be wrong inequality or equals |
| Must be integers |
| M1 for $x(8 p-3 q)$ oe or $-2 y(8 p-3 q)$ oe Or $8 p(x-2 y)$ oe or $-3 q(x-2 y)$ oe | <br>

\hline
\end{tabular}

| Page 3 | Mark Scheme |  | $\frac{\text { Syllabus }}{4024}$ |
| :---: | :---: | :---: | :---: |
| Question | Answers | Mark | Part marks |
| (e) | 1.12 and -2.32 final answer | 4 | B3 for one correct solution or $x=1.1$ to 1.121 and -2.321 to -2.3 <br> If in the form $\frac{p \pm(o r+o r-) \sqrt{q}}{r}$ <br> B1 for $p=-6$ and $r=10$ <br> And B1 for $q=296$ or $\sqrt{q}=17.2 \ldots$ |
| 3 (a) (i) <br> (ii) <br> (b) (i) <br> (ii) | $533.9(0)$ to 534 1760 3.75 $402.5[0]$ or 403 or 402 | 2 | M1 for $32 \times 5.20+0.15 \times 2450$ <br> M1 for $409.6-28 \times 5.20$ [=264] <br> M1 for 'their 264 ' $\div 0.15$ <br> SC1 for an answer of $28.75,28.7,28.8,15$, <br> 3.7, 3.8 or 0.0375 <br> M1 for $\frac{920}{(4+5+7)} \times 7$ |
| 4 (a) (i) <br> (ii) <br> (b) (i) <br> (ii) | $\frac{1}{3}$ $\frac{2}{3}$ <br> 25 numbers completed correctly <br> (a) $\frac{18}{30}$ oe isw <br> (b) $\frac{8}{30}$ oe isw | 1 <br> 1 <br> 1 | After $0+0$ allow B1 for $2 / 6$ and $4 / 6$ Or 0.33 and 0.66 or better <br> After 0+0+0 for (b), <br> If all 36 used $\mathbf{B 1}$ for $18 / 36$ and $10 / 36$ If 35 used, B1 for $18 / 35$ and $9 / 35$ |
| 5 (a) <br> (b) <br> (c) <br> (d) | 78.1 to 78.13 <br> 127.9 to 128 <br> 24.1 to $24.2^{\circ}$ <br> 2900 | 2 | M1 for $\cos 35=\frac{64}{A B}$ or better <br> M1 for $64^{2}+80^{2}+$ or $-(2) \times 64 \times 80 \cos 125$ <br> M1 for $A D^{2}=64^{2}+80^{2}-2 \times 64 \times 80 \cos 125$ <br> M1 for $\frac{\sin A D C}{64}=\frac{\sin 125}{\text { their } 128}$ oe <br> M1 for $\sin A D C=\frac{64 \times \sin 125}{\text { their } 128}$ <br> M1 for $0.5 \times(80+65) \times 40$ |

\begin{tabular}{|c|c|c|c|}
\hline Page 4 \& \multicolumn{2}{|c|}{Mark Scheme} \& \multirow[t]{3}{*}{Syllabus
Part marks
\(6 n\) soi
correct terms seen
\(\frac{n^{2}+3 n}{5 n-12}=6\) or better
\(n^{2}-27 n+72=0\)
ther 3 or 24} \\
\hline Question \& Answers \& Mark \& \\
\hline \begin{tabular}{l}
6 (a) \\
(b) (i) \\
(ii)
\end{tabular} \& \begin{tabular}{l}
\[
23-6 n \text { cao }
\] \\
\(4,10,18,28\) \\
3 and 24
\end{tabular} \& \[
2
\] \& \\
\hline \begin{tabular}{l}
\(7 \quad\) (a) (i) \\
(ii) \\
(iii) \\
(b) (i) \\
(ii) \\
(iii)
\end{tabular} \& \begin{tabular}{l}
9600 cao \\
\(\frac{11}{60}\) cao \\
1440 cao \\
40.1 \\
Correct histogram \\
38 or 39 or 40 or 41
\end{tabular} \& 3

3 \& | M1 for $\frac{360}{60} \times 1600$ oe |
| :--- |
| M1 for $\frac{(144-90)}{360} \times$ their 9600 oe |
| M1 for $\begin{aligned} & 12 \times 17.5+36 \times 25+45 \times 35+33 \times 50 \\ & +24 \times 70 \end{aligned}$ |
| M1 for division by their $(12+36+\ldots+24)$ |
| B1 for 5 bars correct width and position |
| B1 for at least 3 correct heights $k \times(2.4,3.6$, |
| $4.5,1.65,1.2)$ |
| B1 for 5 correct heights | <br>

\hline | 8 |
| :--- |
| (a) (i) |
| (ii) |
| (iii) |
| (iv) |
| (b) (i) |
| (ii) | \& | $\binom{4}{-5}$ |
| :--- |
| 6.4(0) to 6.41 or $\sqrt{41}$ cao $y=-1.25 x+7 \mathrm{oe}$ |
| $(12,-8)$ |
| (a) $\mathbf{b}-\mathbf{a}$ |
| (b) 3a cao |
| (c) $4(\mathbf{b}-\mathbf{a})$ |
| (a) $1: 4$ |
| (b) $1: 15$ | \& | 1 |
| :--- |
| 2 |
| 2 |
| 1 |
| 1 |
| 2 |
| 1 | \& | B1 for gradient $=-1.25$ or $y$-intercept $=+7$ soi in a final equation |
| :--- |
| B1 for one value correct |
| B1 for correct unsimplified $\overrightarrow{C D}$ or for $3(\mathbf{b}-\mathbf{a})$ | <br>

\hline
\end{tabular}

| Page 5 | Mark Scheme |  | $\begin{gathered} \text { Syllabus } \\ \hline 4024 \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| Question | Answers | Mark | Part marks |
| $\begin{array}{ll}9 & \text { (a) } \\ & \text { (b) }\end{array}$ | $\sqrt{15^{2}+6^{2}}=16.15(5 \ldots)$ | 1 | Must be shown to at least 2 d.p. <br> M1 for $\pi \times 6 \times 16.2$ soi by 305.4 <br> M1 for $\pi \times 6^{2}$ soi by 113.1 |
|  | 417 to 419 | 3 |  |
| (c) | 565 to 566 | 2 | M1 for $\frac{1}{3} \times \pi \times 6^{2} \times 15$ or better |
| (d) | 316 to 317 | 2 FT | FT their $(\mathrm{c}) \times 0.56$ evaluated B1 for figs 316(...) or 317(...) or their (c) $\times$ figs 56 evaluated |
| (e) (i) | 18.89 to 18.9 | 2 | M1 for $\sqrt[3]{2}$ or $1.25 \ldots$ seen oe |
| (ii) | 662 to 665 | 2 | M1 for $(\sqrt[3]{2})^{2}$ or $1.58 \ldots$ seen oe |
| 10 (a) | [ $L=] \quad 2\left(x+\frac{50}{x}\right)$ or $2 x+2 \frac{50}{x}$ or $x+x+\frac{50}{x}+\frac{50}{x}$ | 2 | B1 for $\frac{50}{x}$ seen |
| (b) | 41.5 to 41.6, 45 | 2 | B1 for one correct |
| (c) | Correct smooth curve through the eight given points correctly plotted on correctly scaled axes | 3 | $\pm$ half a small square <br> B2 for seven or eight of the given points correctly plotted on their axes or B1 for six of the given points correctly plotted on their axes |
| (d) | 2.8 to $3.2<x<16.8$ to 17.2 | B1 B1 | M1 for attempt to read off two $x$ values at $y=40$ |
| (e) (i) | 27.5 < answer < 28.5 | 1 |  |
| (ii) | 7, 7 cao | 1 |  |
| (f) | 10, 10 cao | 1 |  |


| Page 6 | Mark Scheme |  | $\frac{\text { Syllabus }}{4024}$ |
| :---: | :---: | :---: | :---: |
| $$ | Answers | Mark | Part marks |
|  | $\begin{aligned} & E C=B E \text { or } A C=F E \text { and } \\ & \angle A E C=\angle F B E \text { or } \angle E C A=\angle B E F \end{aligned}$ Two correct reasons for their choices | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Statements and reasons: <br> $E C=B E$; radii <br> $A C=F E$; diameters <br> $\angle A E C=\angle F B E\left[=90^{\circ}\right]$; angle in semicircle <br> $\angle E C A=\angle B E F\left[=60^{\circ}\right]$; equilateral triangle |
|  | Third statement, leading to correct congruence condition i.e. RHS, SAS, SSA | B1 |  |
| (ii) | $B F D$ | 1 |  |
| (iii) | $\angle E B F=\angle D F B=90^{\circ}$ <br> Cointerior/interior/supplementary/allied angles [sum to 180] | $\begin{gathered} 1 \\ 1 \mathrm{dep} \end{gathered}$ | Both $90^{\circ}$ could be marked on diagram |
|  | OR $\angle B E F=\angle E F D=60^{\circ}$ <br> Alternate angles [are equal] | $\begin{gathered} 1 \\ \text { 1dep } \end{gathered}$ | Both $60^{\circ}$ could be marked on diagram |
| (iv) | $120^{\circ}$ | 1 | $120^{\circ}$ could be marked on diagram |
| (b) (i) | 6.126 to 6.13 | 2 | M1 for $\frac{1}{2} \times 4 \times 4 \times \sin 130$ <br> Or $\frac{1}{2} P Q \times$ perpendicular height (numerical) |
| (ii) | 38.2 to 38.3 | 3 | M1 for $\frac{(360-130)}{360} \times \pi \times 4^{2}$ soi by 32.11 or $\frac{130}{360} \times \pi \times 4^{2}$ soi by 18.15 <br> And M1 for 'their major sector area' + 'their triangle area' Or for 'their circle area' - 'their minor sector area' + 'their triangle area' |

