## 4037 ADDITIONAL MATHEMATICS

4037/21
Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

| Page 2 | Mark Scheme | Syllabus |
| :---: | :---: | :---: |

## Mark Scheme Notes

Marks are of the following three types:
M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the $M$ mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Accuracy mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the $M$ marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol $\sqrt{ }$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0 .

B2, 1, 0 means that the candidate can earn anything from 0 to 2 .

| Page 3 | Mark Scheme | Syllabus |
| :---: | :---: | :---: |
|  | GCE O LEVEL - May/June 2013 | 4037 |

The following abbreviations may be used in a mark scheme or used on the scripts:
AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

ISW Ignore Subsequent Working
MR Misread
PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

## Penalties

MR -1 A penalty of MR-1 is deducted from $A$ or $B$ marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all $A$ and $B$ marks then become "follow through V" marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy.

OW $-1,2$ This is deducted from A or B marks when essential working is omitted.
PA -1 This is deducted from A or B marks in the case of premature approximation.
S -1 Occasionally used for persistent slackness - usually discussed at a meeting.
EX -1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.


\begin{tabular}{|c|c|c|c|}
\hline Page 5 \& \multicolumn{2}{|l|}{Mark Scheme GCE O LEVEL - May/June 2013} \& Syllabus \\
\hline 3 \& \begin{tabular}{l}
\[
\frac{\mathrm{d} y}{\mathrm{~d} x}=k \sin x \cos x
\]
\[
k=-8
\] \\
Attempt to find \(x\) when \(y=8\)
\[
\begin{aligned}
\& \mathrm{x}=\frac{\pi}{4}(0.785) \\
\& \text { Uses } \frac{\mathrm{d} y}{\mathrm{~d} t}=\frac{\mathrm{d} y}{\mathrm{~d} x} \times \frac{\mathrm{d} x}{\mathrm{~d} t}
\end{aligned}
\] \\
-0.8 (not rounded)
\end{tabular} \& M1
A1
M1
A1
M1
M1

A1 \& | Must get to $x=$ numerical value |
| :--- |
| $45^{\circ}=\mathbf{A 0}$ (but can still gain next 2 marks) |
| Must use numerical value for $x$ and 0.2 for $\frac{\mathrm{d} x}{\mathrm{~d} t}$ |
| (condone poor notation if correct terms multiplied) | <br>

\hline | (i) |
| :--- |
| (ii) | \& | Idea of modulus correct |
| :--- |
| $\frac{1}{2}$ indicated on $x$-axis |
| 2 indicated on $y$-axis $\frac{2}{3}(0.667)$ |
| Solve $4 x-2=-x$ or $(4 x-2)^{2}=x^{2}$ $\frac{2}{5}$ | \& B1

B1
B1
B1
M1

A1 \& | Two straight lines above and touching $x$-axis |
| :--- |
| Must be a sketch |
| Must be a sketch |
| 0.67 is $\mathbf{B 0}$ |
| As far as $x=$ numerical value |
| SC: If drawn then B1, B2 for exact answers only | <br>

\hline | (i) |
| :--- |
| (ii) | \& \[

$$
\begin{aligned}
& (Q R=P S=) \frac{96-3 x}{2} \\
& \text { Area }=\left(\frac{96-3 x}{2}\right) \times x \\
& \frac{\mathrm{~d} A}{\mathrm{~d} x}=\frac{96-6 x}{2} \text { or } 48-3 x \text { o.e. } \\
& \text { Solving } \frac{\mathrm{d} A}{\mathrm{~d} x}=\frac{96-6 x}{2}=0 \\
& x=16 \\
& A=384 \text { and state maximum }
\end{aligned}
$$
\] \& B1

B1
B1
M1
A1

A1 \& | Can be implied by next statement |
| :--- |
| AG |
| As far as $x=$ numerical value | <br>

\hline
\end{tabular}

| Page 6 | $\frac{\text { Mark Scheme }}{\text { GCE O LEVEL - May/June } 2013}$ |  | Syllabus |
| :---: | :---: | :---: | :---: |
| 6 | Applies quotient rule correctly $\begin{aligned} & \frac{(x-2) 2 x-\left(x^{2}+8\right)}{(x-2)^{2}} \\ & y=12 \end{aligned}$ <br> Uses $m_{1} m_{2}=-1$ <br> $\left(\right.$ Gradient normal $\left.=\frac{1}{2}\right)$ <br> Uses equation of line for normal $y-12=\frac{1}{2}(x-4) \quad \text { or } \quad y=\frac{1}{2} x+10$ | M1 <br> A1 <br> B1 <br> M1 <br> M1 <br> A1 | or product rule $2 x(x-2)^{-1}-\left(x^{2}+8\right)(x-2)^{-}$ <br> If uses $y=m x+c$ must find $c$ for M1 |
| $7 \begin{array}{ll}\text { 7 } & \text { (i) } \\ & \\ & \text { (ii) }\end{array}$ | $64+192 x+240 x^{2}+160 x^{3}$ mark final answer | $\underset{\mathbf{0}}{\mathbf{B 3}, \mathbf{2},}$ | 3 terms correct earn B2; 2 terms correct earn B1 Can be earned in (ii); SC2 correct but unsimplified |
|  | Multiply out $(1+3 x)(1-x)$ $1+2 x-3 x^{2} \text { o.e. }$ | M1 <br> A1 |  |
|  | (1) $\times(160)+(2) \times(240)+(-3) \times(192)$ o.e. | M1 | 3 terms |
|  |  | A1 |  |
|  | Or <br> Multiply out $(1-x)\left(64+192 x+240 x^{2}+160 x^{3}\right)$ | [M1 | May be other variations: for first M1 find $x^{2}$ term or $x^{3}$ term |
|  | ... $48 x^{2}-80 x^{3} \ldots$...e. | A1 |  |
|  | Multiply by $1+3 x$ | M1 | for second M1 must produce all relevant terms |
|  |  | A1] |  |
|  | $\begin{aligned} & \text { Or } \\ & (1+3 x)\left(64+192 x+240 x^{2}+160 x^{3}\right) \end{aligned}$ | [M1 |  |
|  | $\ldots 816 x^{2}+880 x^{3} \ldots \text {...e. }$ | A1 |  |
|  | Multiply by $1-x$ | M1 |  |
|  | 64 | A1] |  |


| Page 7 | Mark Scheme | Syllabus |
| :---: | :---: | :---: |
|  | GCE O LEVEL - May/June 2013 | 4037 |


| 8 | Eliminates $y$ (or $x$ ) and full attempt at expansion $4 x^{2}-8 x-96=0 \quad \text { or } y^{2}+12 y-64=0$ <br> Factorise 3 term relevant quadratic $\begin{array}{ll} x=-4 \text { and } 6 & \text { or } y=-16 \text { and } 4 \\ y=-16 \text { and } 4 & \text { or } x=-4 \text { and } 6 \end{array}$ <br> Uses Pythagoras for relevant points <br> 22.4 or $\sqrt{500}$ or $10 \sqrt{5}$ | M1 <br> A1 <br> M1 <br> A1 <br> A1 $\sqrt{ }$ <br> M1 <br> A1 | Or use correct formula <br> cao |
| :---: | :---: | :---: | :---: |
| 9 <br> (i) <br> (ii) <br> (iii) | Attempt to solve 3 term quadratic $\begin{aligned} & -3 \text { and } 8 \\ & -3, x, 8 \\ & 4, x(, 12) \\ & S \cup T=-3, x, 12 \\ & S \cap T=4, x, 8 \text { or } \\ & S^{\prime}=-5, x<-3,8<x, 12 \text { and } \\ & T^{\prime}=-5, x<4 \\ & -5, x<4 \\ & 8<x, 12 \end{aligned}$ | M1 <br> A1 <br> A1 <br> B1 <br> B1 <br> B1 <br> B1 $\sqrt{ }$ <br> B1 $\sqrt{ }$ | Condone $-3, x$ AND $x, 8$ <br> Penalise confusion over , and < (or . and >) once only <br> their 4 <br> their 8 (Ignore AND/OR etc.) |



| Page 9 | Mark Scheme |  | Syllabus |
| :---: | :---: | :---: | :---: |
| $12 \quad \begin{array}{rr}\text { (i) } \\ & \\ & \\ & \text { (ii) }\end{array}$ | $\mathrm{f}(3)=(27+9+3 a+b)=0$ or $3 a+b=-36$ | M1 | Equate $f(3)$ to 0 |
|  | $\mathrm{f}(-1)=(-1+1-a+b)=20$ or $-a+b=20$ | M1 | Equate $\mathrm{f}(-1)$ to 20 |
|  | Solve equations | M1 |  |
|  | $a=-14, b=6$ | A1 | If uses $b=6$ then $\mathbf{M 0} \mathbf{0} \mathbf{A 0}$ Need both values for A1 |
|  | Find quadratic factor | M1 | If division, must be complete with first 2 terms correct If writes down, must be $\left(x^{2}+k x-2\right)$ |
|  | $x^{2}-4 x-2$ | A1 |  |
|  | Use quadratic formula or completing square on relevant 3 term quadratic | M1 | If completing square, must reach $\left(x+\frac{k}{2}\right)^{2}=2 \pm\left(\frac{k}{2}\right)^{2}$ |
|  | $\frac{-4 \pm \sqrt{16+8}}{2}$ or better | A1 $\sqrt{ }$ |  |
|  | $-2 \pm \sqrt{6}$ isw | A1 | cao |

