

**CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**GCE Ordinary Level**

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## **MARK SCHEME for the October/November 2013 series**

### **4024 MATHEMATICS (SYLLABUS D)**

**4024/12**

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

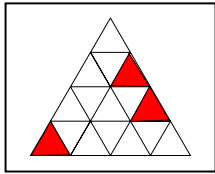
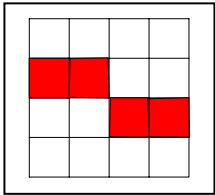
Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

|        |                                     |          |
|--------|-------------------------------------|----------|
| Page 2 | Mark Scheme                         | Syllabus |
|        | GCE O LEVEL – October/November 2013 | 4024     |

**Abbreviations**

- cao correct answer only
- cso correct solution only
- dep dependent
- ft follow through after error
- isw ignore subsequent working
- oe or equivalent
- SC Special Case
- www without wrong working
- soi seen or implied

| Question | Answers   | Mark | Part marks   |
|----------|---|------|--|
| 1 (a)    | 2.38 oe   | 1    |  |
| (b)      | 80 (.0)(0)  | 1    |  |
| 2 (a)    | $1\frac{9}{20}$   | 1    |  |
| (b)      | 0.0602  | 1    |  |
| 3 (a)    | -7  | 1    |  |
| (b)      | $\frac{x+6}{2}$ oe  | 1    |  |
| 4 (a)    | (0)3 hours 48 minutes   | 1    |  |
| (b)      | $\frac{2}{5}$ 44% $\frac{4}{9}$   | 1    |  |
| 5 (a)    |  | 1    |  |
| (b)      |  | 1    |  |
| 6        | 8   | 2    | <b>B1</b> for “k” = 40<br>or <b>M1</b> either for $20 \times 2 = 5y$ oe; or for<br>(their $k$ )/5, when $y = “k”/x$ used |
| 7 (a)    | $3.5 \times 10^7$   | 1    |  |
| (b)      | $1.4 \times 10^{-6}$  | 1    |  |
| 8        | $\frac{3}{7}$   | 2    | <b>B1</b> for $7x = c$ , or for $\frac{7x}{c} = C$ , or for<br>$cx = 3C$ ; where $c$ and $C$ are integers<br>(not 0).    |

|               |  |                 |
|---------------|--|-----------------|
| <b>Page 3</b> | <b>Mark Scheme</b>                         | <b>Syllabus</b> |
|               | <b>GCE O LEVEL – October/November 2013</b> | <b>4024</b>     |

|               |  |   |   |
|---------------|--|---|---|
| <b>9</b>      | 200  | 2 | Dep. on <b>three</b> correct approximations seen.<br><b>B1</b> for either $\sqrt{35.78} \approx 6$ , or $\sqrt[3]{1005} \approx 10$ |
| <b>10</b>     | Any number <b>between</b> 4 and 5          | 2 | <b>B1</b> for $x < 5$ , or for $5 > x$ seen.<br>This may appear as, e.g., $4 < x < 5$ .   |
| <b>11 (a)</b> | 45.5°                                      | 1 | <b>C1</b> for $151 < x \leq 151.2$<br>or <b>M1</b> for $360 - 46.5 - 162.5$<br>or <b>M1</b> for $360 - 46 - 162 - 1$                |
| <b>(b)</b>    | 151°                                       | 2 |   |
| <b>12 (a)</b> | $\frac{9}{25}$                             | 1 |   |
| <b>(b)</b>    | $\frac{3}{t^3}$ or $3t^{-3}$               | 1 |   |
| <b>(c)</b>    | $\frac{x^2}{3y}$ or $\frac{1}{3}x^2y^{-1}$ | 1 |   |
| <b>13</b>     | Both $x = \frac{1}{2}$ and $y = -4$        | 3 | <b>C2</b> for either $x$ or $y$ correct WWW<br>or <b>C1</b> for a pair of values that satisfy either equation                       |
| <b>14 (a)</b> | 1.35                                       | 1 |   |
| <b>(b)</b>    | 1.1  | 1 |   |
| <b>(c)</b>    | 104  | 1 |   |
| <b>15 (a)</b> | B C D                                      | 1 |   |
| <b>(b)</b>    | E  | 1 |   |
| <b>(c)</b>    | $y < \frac{1}{2}x$ oe                      | 1 |   |

|        |                                     |          |
|--------|-------------------------------------|----------|
| Page 4 | Mark Scheme                         | Syllabus |
|        | GCE O LEVEL – October/November 2013 | 4024     |

|        |  |                |  |
|--------|--|----------------|--|
| 16     | 76   | 3              | <p>Dep. on volume expressions of <math>a^3</math>.</p> <p><b>C2</b> for <math>76a</math>, or <math>76a^2</math>, or <math>76(\pi)a^3</math>,<br/>or <math>\frac{76}{a}</math>, or <math>\frac{76}{a^2}</math>, or <math>\frac{76}{a^3}</math></p> <p><b>B1</b> for a 3-spheres volume of<br/><math>\frac{4}{3}\pi \times (2a)^3 \times 3</math> or <math>32\pi a^3</math></p> <p>and <b>B1</b> for a cylinder volume of<br/><math>\pi \times (3a)^2 \times 12a</math> or <math>108\pi a^3</math>;</p> <p>or<br/><b>B1</b> for <b>both</b> <math>108\pi\dots</math> and <math>32\pi\dots</math> without <math>a^3</math>.</p> |
| 17 (a) | $(5t - 2)(5t + 2)$   | 1              | <p><b>B1</b> for partial factorisation <math>4x(2y + 1)</math><br/>or<br/><math>-3(2y + 1)</math> or <math>2y(4x - 3)</math> seen</p>  |
| (b)    | $2r^2(3H - h)$   | 1              |  |
| (c)    | $(4x - 3)(2y + 1)$   | 2              |  |
| 18 (a) | 16   | 1              |  |
| (b)    | Rectangle, base 2 to 3, height 6 units<br>Rectangle, base 7 to 9, height 2 units | 1<br>1         |  |
| (c)    | ft $\frac{15}{31 + \text{their}(p)}$   | 1 $\checkmark$ |  |
| 19 (a) | (2, 1)   | 1              | <p><b>C1</b> for <math>(\sqrt{\quad}) 52</math></p> <p>or <b>M1</b> for <math>6^2 + (-4)^2</math>, or for <math>6^2 + (4)^2</math>,<br/>etc.</p>   |
| (b)    | $-\frac{2}{3}$ or any equiv. value   | 1              |  |
| (c)    | 13   | 2              |  |

|     |                |   |           |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|-----|----------------|---|-----------|--|----|----|----|----|---|---|---|---|---|----|----|----|----|----|---|----|---|----|----|----|----|---|----|----|---|----|----|----|---|----|----|----|---|----|----|---|----|----|----|----|---|----|---|----|----|----|----|----|---|
| 20  | (a)            | Reflection<br>$y = x$ oe  | 1<br>1    | but lost if more than one trans<br>indep. – but lost if more than one<br>transf. named   |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (b) (i)        | Triangle with vertices $(-1, 0), (-3, 0), (-3, 1)$                                    | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (ii)           | $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$                                       | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 21  | (a)            | 1   | 1         | <p><b>M1</b> for <math>\frac{3}{6} \times \frac{2}{5} \times \frac{2}{6} \times \frac{1}{5}</math> oe</p> <p>or for any complete possibility diagram such as the one below, <b>correctly used</b>.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td></td> <td>2</td> <td>3</td> <td>3</td> <td>4</td> <td>4</td> <td>4</td> </tr> <tr> <td>2</td> <td>–</td> <td>23</td> <td>23</td> <td>24</td> <td>24</td> <td>24</td> </tr> <tr> <td>3</td> <td>32</td> <td>–</td> <td>33</td> <td>34</td> <td>34</td> <td>34</td> </tr> <tr> <td>3</td> <td>32</td> <td>33</td> <td>–</td> <td>34</td> <td>34</td> <td>34</td> </tr> <tr> <td>4</td> <td>42</td> <td>43</td> <td>43</td> <td>–</td> <td>44</td> <td>44</td> </tr> <tr> <td>4</td> <td>42</td> <td>43</td> <td>43</td> <td>44</td> <td>–</td> <td>44</td> </tr> <tr> <td>4</td> <td>42</td> <td>43</td> <td>43</td> <td>44</td> <td>44</td> <td>–</td> </tr> </table> |    | 2  | 3  | 3  | 4 | 4 | 4 | 2 | – | 23 | 23 | 24 | 24 | 24 | 3 | 32 | – | 33 | 34 | 34 | 34 | 3 | 32 | 33 | – | 34 | 34 | 34 | 4 | 42 | 43 | 43 | – | 44 | 44 | 4 | 42 | 43 | 43 | 44 | – | 44 | 4 | 42 | 43 | 43 | 44 | 44 | – |
|     |                | 2   | 3         |  | 3  | 4  | 4  | 4  |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | 2              | –   | 23        |  | 23 | 24 | 24 | 24 |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 3   | 32             | –   | 33        | 34   | 34 | 34 |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 3   | 32             | 33  | –         | 34   | 34 | 34 |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 4   | 42             | 43  | 43        | –  | 44 | 44 |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 4   | 42             | 43  | 43        | 44   | –  | 44 |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 4   | 42             | 43  | 43        | 44   | 44 | –  |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| (b) | $\frac{1}{15}$ | 1   |           |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| (c) | $\frac{4}{15}$ | 2   |           |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 22  | (a)            | $48^\circ$  | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (b)            | $66^\circ$  | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (c)            | $24^\circ$  | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (d)            | $35^\circ$  | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 23  | (a)            | $15^2 - 1^2 = 8 \times (1 + 2 + 3 + 4 + 5 + 6 + 7)$                                   | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (b)            | $(2n + 1)^2 - 1^2$ oe   | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (c)            | $(2n + 1)^2 = 4n^2 + 4n + 1$ or<br>$(2n + 1)^2 - 1^2 = 4n^2 + 4n$ , or $(2n)(2n + 2)$ | <b>B1</b> |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     |                | Division of both sides by 8 and result obtained correctly                             | <b>M1</b> |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
| 24  | (a)            | $96^\circ$ to $98^\circ$  | 1         | dep.on both (b) marks  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (b) (i)        | acceptable perpendicular bisector of $AB$   | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (ii)           | acceptable bisector of angle $ABC$  | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |
|     | (c)            | 10 to 10.3  | 1         |  |    |    |    |    |   |   |   |   |   |    |    |    |    |    |   |    |   |    |    |    |    |   |    |    |   |    |    |    |   |    |    |    |   |    |    |   |    |    |    |    |   |    |   |    |    |    |    |    |   |

|        |                                     |          |
|--------|-------------------------------------|----------|
| Page 6 | Mark Scheme                         | Syllabus |
|        | GCE O LEVEL – October/November 2013 | 4024     |

|         |  |                 |   |
|---------|--|-----------------|---|
| 25 (a)  | 16   | 1               |   |
| (b)     | 150  | 1               |   |
| (c)     | 45 WWW or ft $\frac{750 - \text{their}(b)}{20} + 15$   | 2 $\frac{1}{2}$ | <b>C1</b> for $\frac{750 - \text{their}(b)}{20}$<br>or <b>M1</b> for $\frac{1}{2} \times (k + k - 15) \times 20 = 750$<br>or <b>M1</b> for $20(k - 15) + \text{their}(b) = 750$<br>oe |
| (d)     | 10   | 1               |   |
| 26 (a)  | Establishing, with reasons, that two pairs of angles are equal; and a conclusion (or an introductory statement), that the triangles are similar. e.g.<br>$\hat{A}BD = \hat{B}DC$ (alternate angles)<br>$\hat{A}DB = \hat{B}CD$ (given)<br>Since two angles are equal, triangles $ABD$ and $BDC$ are similar. | 2               | <b>B1</b> for $\hat{A}BD = \hat{B}DC$ , <b>with</b> mention of alternate angles   |
| (b) (i) | 6.3  | 2               | <b>B1</b> for $\frac{BC}{4.2} = \frac{6}{4}$ oe   |
| (ii)    | $\frac{4}{9}$  | 1               |   |